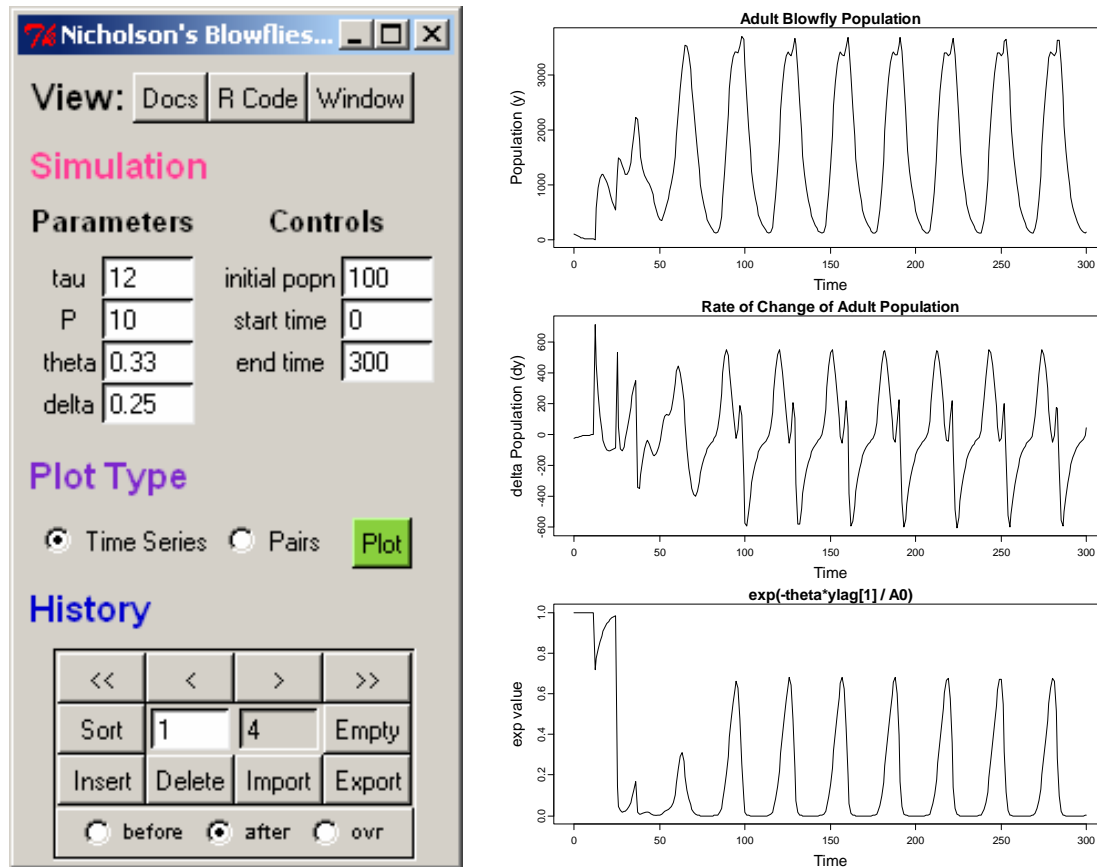


Extract from the user's guide PBSddesolve-UG.pdf found in the directory  
 .../library/PBSddesolve/doc. For further information, please see the complete guide.

## 4.2 Blowflies – (DDE Example)



**Figure 2.** Nicholson's blowflies model demonstration (included in Simon Wood's Solv95 User Manual as an example of solving a DDE).

As an example with a delay, Wood (1999) suggested a blowfly population model for adults  $A(t)$  at time  $t$ :

$$\frac{dA}{dt} = \begin{cases} -\delta A(t), & t < t_0 + \tau; \\ PA(t - \tau)e^{-\theta A(t - \tau)/A_0} - \delta A(t), & t \geq t_0 + \tau; \end{cases}$$

$$A(t_0) = A_0.$$

Here  $\tau$  is the development time from egg to adult,  $P$  is the net production rate determined by adult fecundity and egg survival to adulthood,  $\theta$  is a parameter determining how quickly fecundity declines with an increasing adult population,  $\delta$  is the adult death rate, and  $t_0$  is the initial time when  $A(t)$  starts with the value  $A_0$ . We assume that  $A(t) = 0$  for  $t < t_0$ . In our

formulation, the differential equation also includes the parameter  $A_0$ , so that  $\theta$  becomes dimensionless. Essentially,  $A_0$  sets the scale for  $A(t)$ .

The GUI in Figure 2 allows the four parameters  $(\tau, P, \theta, \delta)$  to be adjusted, along with the initial conditions  $(t_0, A_0)$  and the final time  $t_1$ . The graph at the left shows three panels:  $A(t)$ ,  $dA(t)/dt$ , and  $e^{-\theta A(t-\tau)/A_0}$ . In this case, a key portion of the R code is:

```
myGrad <- function(t, y) {  
  if (t-t0 >= tau) ylag <- pastvalue(t-tau)  
  else ylag <- 0  
  yexp <- exp(-theta*ylag[1]/A0)-delta*y[1]  
  yp <- P*ylag[1]*yexp  
  return( list(yp, c(dy=yp, exp=yexp)) ) }
```

where values of tau, P, theta, delta, t0, and A0 come from the GUI.