# Package 'OutcomeWeights'

November 21, 2024

Type Package

Title Outcome Weights of Treatment Effect Estimators

Version 0.1.0

**Description** Many treatment effect estimators can be written as weighted outcomes. These weights have established use cases like checking covariate balancing via pack-

ages like 'cobalt'.

This package takes the original estimator objects and outputs these outcome weights. It builds on the general framework of Knaus (2024) <doi:10.48550/arXiv.2411.11559>. This version is compatible with the 'grf' package and provides an internal implementation of Double Machine Learning.

License GPL-3

**Encoding** UTF-8

URL https://github.com/MCKnaus/OutcomeWeights

BugReports https://github.com/MCKnaus/OutcomeWeights/issues

Imports ggplot2, grf, methods

LinkingTo Rcpp, RcppArmadillo

RoxygenNote 7.3.2

Suggests testthat (>= 3.0.0)

Config/testthat/edition 3

NeedsCompilation yes

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**Repository** CRAN

Date/Publication 2024-11-21 08:00:10 UTC

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dml\_with\_smoother Double ML estimators with outcome smoothers

# Description

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Existing Double ML implementations are too general to easily extract smoother matrices required to be compatible with the get\_forest\_weights() method. This motivates yet another Double ML implementation.

# Usage

```
dml_with_smoother(
    Y,
    D,
    X,
    Z = NULL,
    estimators = c("PLR", "PLR_IV", "AIPW_ATE", "Wald_AIPW"),
    smoother = "honest_forest",
    n_cf_folds = 5,
    n_reps = 1,
    ...
)
```

Numeric vector containing the outcome variable.
Optional binary treatment variable.
Covariate matrix with N rows and p columns.
Optional binary instrumental variable.

estimators	String (vector) indicating which estimators should be run. Current menu: c("PLR","PLR_IV","AIPW_AI
smoother	Indicate which smoother to be used for nuisance parameter estimation. Currently only available option "honest_forest" from the <b>grf</b> package.
n_cf_folds	Number of cross-fitting folds. Default is 5.
n_reps	Number of repetitions of cross-fitting. Default is 1.
	Options to be passed to smoothers.

#### Value

A list with three entries:

- results: a list storing the results, influence functions, and score functions of each estimator
- NuPa.hat: a list storing the estimated nuisance parameters and the outcome smoother matrices

#### References

Chernozhukov, V., Chetverikov, D., Demirer, M., Duflo, E., Hansen, C., Newey, W., & Robins, J. (2018). Double/debiased machine learning for treatment and structural parameters. The Econometrics Journal, 21(1), C1-C68.

Knaus, M. C. (2024). Treatment effect estimators as weighted outcomes, https://arxiv.org/ abs/2411.11559.

#### Examples

```
# Sample from DGP borrowed from grf documentation
n = 200
p = 5
X = matrix(rbinom(n * p, 1, 0.5), n, p)
Z = rbinom(n, 1, 0.5)
Q = rbinom(n, 1, 0.5)
W = Q * Z
tau = X[, 1] / 2
Y = rowSums(X[, 1:3]) + tau * W + Q + rnorm(n)
# Run outcome regression and extract smoother matrix
# Run DML and look at results
dml = dml_with_smoother(Y,W,X,Z)
results_dml = summary(dml)
plot(dml)
# Get weights
omega_dml = get_outcome_weights(dml)
# Observe that they perfectly replicate the original estimates
all.equal(as.numeric(omega_dml$omega %*% Y),
```

```
as.numeric(as.numeric(results_dml[,1])))
```

# The weights can then be passed to the cobalt package for example.

#### Description

This is a generic method for getting outcome weights. It calculates the outcome weights for objects created by other packages. See get\_outcome\_weight.<compatible\_fct> in the package documentation for compatible functions.

#### Usage

```
get_outcome_weights(object, ...)
```

#### Arguments

object	An object, obtained from other packages.	
	Additional arguments specific to object class implementations. See mentation which object requires which additional arguments.	e the docu-

#### Value

A list of at least these components:

- omega: matrix (number of point estimates x number of estimation units) of outcome weights
- treat: the treatment indicator to make it compatible with the cobalt package

#### References

Knaus, M. C. (2024). Treatment effect estimators as weighted outcomes, https://arxiv.org/ abs/2411.11559.

#### Description

Post-estimation command to extract outcome weights for causal forest implemented via the causal\_forest function from the **grf** package.

# Usage

```
## S3 method for class 'causal_forest'
get_outcome_weights(
    object,
    ...,
    S,
    newdata = NULL,
    S.tau = NULL,
    target = "CATE",
    checks = TRUE
)
```

#### ,

# Arguments

Pass potentially generic get_outcome_weights options.
A smoother matrix reproducing the outcome predictions used in building the instrumental_forest. Obtained by calling get_forest_weights() for the regression_forest object producing the outcome predictions.
Corresponds to newdata option in predict.causal_forest. If NULL, out-of- bag outcome weights, otherwise for those for the provided test data returned.
Required if target != "CATE", then S.tau is the CATE smoother obtained from running get_outcome_weights() with target == "CATE".
Target parameter for which outcome weights should be extracted. Currently $c("CATE", "ATE")$ implemented.
Default TRUE checks whether weights numerically replicate original estimates. Only set FALSE if you know what you are doing and need to save computation time.

# Value

get\_outcome\_weights object with omega containing weights and treat the treatment

#### References

Athey, S., Tibshirani, J., & Wager, S. (2019). Generalized random forest. The Annals of Statistics, 47(2), 1148-1178.

Knaus, M. C. (2024). Treatment effect estimators as weighted outcomes, https://arxiv.org/ abs/2411.11559.

# Examples

```
# Sample from DGP borrowed from grf documentation
n = 500
p = 10
X = matrix(rnorm(n * p), n, p)
W = rbinom(n, 1, 0.5)
```

```
Y = pmax(X[, 1], 0) * W + X[, 2] + pmin(X[, 3], 0) + rnorm(n)
# Run outcome regression and extract smoother matrix
forest.Y = grf::regression_forest(X, Y)
Y.hat = predict(forest.Y)$predictions
outcome_smoother = grf::get_forest_weights(forest.Y)
# Run causal forest with external Y.hats
c.forest = grf::causal_forest(X, Y, W, Y.hat = Y.hat)
# Predict on out-of-bag training samples.
cate.oob = predict(c.forest)$predictions
# Predict using the forest.
X.test = matrix(0, 101, p)
X.test[, 1] = seq(-2, 2, length.out = 101)
cate.test = predict(c.forest, X.test)$predictions
# Calculate outcome weights
omega_oob = get_outcome_weights(c.forest,S = outcome_smoother)
omega_test = get_outcome_weights(c.forest,S = outcome_smoother,newdata = X.test)
# Observe that they perfectly replicate the original CATEs
all.equal(as.numeric(omega_oob$omega %*% Y),
          as.numeric(cate.oob))
all.equal(as.numeric(omega_test$omega %*% Y),
          as.numeric(cate.test))
# Also the ATE estimates are perfectly replicated
omega_ate = get_outcome_weights(c.forest,target = "ATE",
                                S = outcome_smoother,
                                S.tau = omega_oob$omega)
all.equal(as.numeric(omega_ate$omega %*% Y),
          as.numeric(grf::average_treatment_effect(c.forest, target.sample = "all")[1]))
```

# The omega weights can be plugged into balancing packages like cobalt

#### Description

Post-estimation command to extract outcome weights for double ML run with an outcome smoother.

#### Usage

```
## S3 method for class 'dml_with_smoother'
get_outcome_weights(object, ..., all_reps = FALSE)
```

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#### Arguments

object	An object of class dml_with_smoother, i.e. the result of running dml_with_smoother.
	Pass potentially generic get_outcome_weights options.
all_reps	If TRUE, outcomes weights of each repetitions passed. Default FALSE.

#### Value

- If all\_reps == FALSE: get\_outcome\_weights object
- If all\_reps == TRUE: additionally list omega\_all\_reps: A list containing the outcome weights of each repetition.

#### References

Knaus, M. C. (2024). Treatment effect estimators as weighted outcomes, https://arxiv.org/ abs/2411.11559.

# Description

Post-estimation command to extract outcome weights for instrumental forest implemented via the instrumental\_forest function from the **grf** package.

#### Usage

```
## S3 method for class 'instrumental_forest'
get_outcome_weights(object, ..., S, newdata = NULL, checks = TRUE)
```

object	An object of class instrumental_forest, i.e. the result of running instrumental_forest.
	Pass potentially generic get_outcome_weights options.
S	A smoother matrix reproducing the outcome predictions used in building the instrumental_forest. Obtained by calling get_forest_weights() for the regression_forest object producing the outcome predictions.
newdata	Corresponds to newdata option in predict.instrumental_forest. If NULL, out-of-bag outcome weights, otherwise for those for the provided test data re-turned.
checks	Default TRUE checks whether weights numerically replicate original estimates. Only set FALSE if you know what you are doing and want to save computation time.

#### Value

get\_outcome\_weights object with omega containing weights and treat the treatment

#### References

Athey, S., Tibshirani, J., & Wager, S. (2019). Generalized random forest. The Annals of Statistics, 47(2), 1148-1178.

Knaus, M. C. (2024). Treatment effect estimators as weighted outcomes, https://arxiv.org/ abs/2411.11559.

#### Examples

```
# Sample from DGP borrowed from grf documentation
n = 2000
p = 5
X = matrix(rbinom(n * p, 1, 0.5), n, p)
Z = rbinom(n, 1, 0.5)
Q = rbinom(n, 1, 0.5)
W = Q * Z
tau = X[, 1] / 2
Y = rowSums(X[, 1:3]) + tau * W + Q + rnorm(n)
# Run outcome regression and extract smoother matrix
forest.Y = grf::regression_forest(X, Y)
Y.hat = predict(forest.Y)$predictions
outcome_smoother = grf::get_forest_weights(forest.Y)
# Run instrumental forest with external Y.hats
iv.forest = grf::instrumental_forest(X, Y, W, Z, Y.hat = Y.hat)
# Predict on out-of-bag training samples.
iv.pred = predict(iv.forest)$predictions
omega_if = get_outcome_weights(iv.forest, S = outcome_smoother)
# Observe that they perfectly replicate the original CLATEs
all.equal(as.numeric(omega_if$omega %*% Y),
          as.numeric(iv.pred))
```

NuPa\_honest\_forest Nuisance parameter estimation via honest random forest

#### Description

This function estimates different nuisance parameters using the honest random forest implementation of the 'grf' package

# NuPa\_honest\_forest

# Usage

```
NuPa_honest_forest(
NuPa = c("Y.hat", "Y.hat.d", "Y.hat.z", "D.hat", "D.hat.z", "Z.hat"),
X,
Y = NULL,
D = NULL,
Z = NULL,
n_cf_folds = 5,
n_reps = 1,
cluster = NULL,
progress = FALSE,
...
```

# Arguments

NuPa	String vector specifying the nuisance parameters to be estimated. Currently supported: c("Y.hat", "Y.hat.d", "Y.hat.z", "D.hat", "D.hat.z", "Z.hat")
Х	Covariate matrix with N rows and p columns.
Υ	Optional numeric vector containing the outcome variable.
D	Optional binary treatment variable.
Z	Optional binary instrumental variable.
n_cf_folds	Number of cross-fitting folds. Default is 5.
n_reps	Number of repetitions of cross-fitting. Default is 1.
cluster	Optional vector of cluster variable if cross-fitting should account for clusters.
progress	If TRUE, progress of nuisance parameter estimation reported.
	Options passed to the regression_forest.

# Value

List of two lists.

- predictions contains the requested nuisance parameters
- smoothers contains the smoother matrices of requested outcome nuisance parameters
- cf\_mat Array of dimension n\_reps x N x n\_cf\_folds storing indicators representing the folds used in estimation.

# References

Wager, S., & Athey, S. (2018). Estimation and inference of heterogeneous treatment effects using random forests. Journal of the American Statistical Association, 113(523), 1228-1242.

pive\_weight\_maker Outcome weights maker for pseudo-IV estimators.

# Description

This is a generic function taking pseudo-instrument, pseudo-treatment and the transformation matrix as inputs and returning outcome weights

#### Usage

```
pive_weight_maker(Z.tilde, D.tilde, T_mat)
```

# Arguments

Z.tilde	Numeric vector of pseudo-instrument outcomes.
D.tilde	Numeric vector of pseudo-treatment.
T_mat	Transformation matrix

# Value

A vector of outcome weights.

#### References

Knaus, M. C. (2024). Treatment effect estimators as weighted outcomes, soon on 'arXiv'.

plot.dml\_with\_smoother

plot method for class dml\_with\_smoother

# Description

plot method for class dml\_with\_smoother

#### Usage

```
## S3 method for class 'dml_with_smoother'
plot(x, ..., alpha = 0.05, contrast = FALSE)
```

х	Object of class dml_with_smoother.
	Pass generic plot options.
alpha	Significance level for confidence intervals (default 0.05).
contrast	Shows the differences between the coefficients.

prep\_cf\_mat

#### Value

ggplot with point estimates and confidence intervals.

prep_cf_mat	Creates matrix of binary cross-fitting fold indicators (N x # cross-
	folds)

# Description

Creates matrix of binary cross-fitting fold indicators (N x # cross-folds)

#### Usage

prep\_cf\_mat(n, cf, w\_mat = NULL, cl = NULL)

# Arguments

n	Number of observations.
cf	Number of cross-fitting folds.
w_mat	Optional logical matrix of treatment indicators (N x T+1). If specified, cross- fitting folds will preserve the treatment ratios from full sample.
cl	Optional vector of cluster variable if cross-fitting should account for clusters.

# Value

Logical matrix of cross-fitting folds (N x # folds).

# Description

Calculates standardized mean differences between treated and controls and towards target means for an outcome weights matrix with potentially many rows like for CATEs.

# Usage

```
standardized_mean_differences(X, treat, omega, target = NULL)
```

#### Arguments

Х	Covariate matrix with N rows and p columns.
treat	Binary treatment variable.
omega	Outcome weights matrix with dimension number of weight vectors for which balancing should be checked x number of training units.
target	Optional matrix with dimension number of weight vectors for which balanc- ing should be checked x p indicating the target values the covariates should be balanced towards. If NULL, average of X used as target of ATE.

# Value

3D-array of dimension  $p \ge 6 x$  number of weight vectors for which balancing should be checked where the second dimension provides the following quantities:

- "Mean 0": The weighted control mean
- "Mean 1": The weighted treated mean
- "SMD balancing": Standardized mean differences for covariate balancing (Mean 1 Mean 0) / sd(X)
- "SMD targeting 0": Standardized mean difference to assess targeting of control (Mean 0 target) / sd(X)
- "SMD targeting 1": Standardized mean difference to assess targeting of treated (Mean 1 target) / sd(X)

# References

Rosenbaum, P. R., & Rubin, D. B. (1984). Reducing bias in observational studies using subclassification on the propensity score. Journal of the American Statistical Association, 79 (387), 516–524.

summary.dml\_with\_smoother

summary method for class dml\_with\_smoother

#### Description

summary method for class dml\_with\_smoother

#### Usage

```
## S3 method for class 'dml_with_smoother'
summary(object, contrast = FALSE, quiet = FALSE, ...)
```

object	Object of class dml_with_smoother.
contrast	Tests the differences between the coefficients.
quiet	If TRUE, results are passed but not printed.
•••	further arguments passed to printCoefmat

# Value

Invisible matrix with estimator(s) in the rows and c("Estimate", "SE", "t", "p") in the columns.

summary.get\_outcome\_weights

summary method for class outcome\_weights

# Description

Calculates several summary measures of potentially many outcome weights.

# Usage

```
## S3 method for class 'get_outcome_weights'
summary(object, quiet = FALSE, digits = 4, epsilon = 1e-04, ...)
```

# Arguments

object	get_outcome_weights object.
quiet	If TRUE, results are passed but not printed.
digits	Number of digits to be displayed. Default 4.
epsilon	Threshold below which in absolute values non-zero but small values should be displayed as <
	further arguments passed to printCoefmat

#### Value

3D-array of dimension

- c("Control","Treated") x
- number of point estimates x
- c("Minimum weight", "Maximum weight", "% Negative", "Sum largest 10%", "Sum of weights", "Sum of absolute weights")

summary.standardized\_mean\_differences

summary method for class standardized\_mean\_differences

#### Description

Calls a C++ function to quickly summarize potentially many standardized mean differences.

# Usage

## S3 method for class 'standardized\_mean\_differences'
summary(object, ...)

#### Arguments

object	Object of class standardized_mean_differences.
	further arguments passed to summary method.

#### Value

3D-array of dimension

- c("Maximum absolute SMD","Mean absolute SMD", "Median absolute SMD", / % of absolute SMD > 20", "# / % of absolute SMD > 10", "# / % of absolute SMD > 5") x
- c("Balancing","Targeting") x
- number of weight vectors for which balancing should be checked

#### References

Rosenbaum, P. R., & Rubin, D. B. (1984). Reducing bias in observational studies using subclassification on the propensity score. Journal of the American Statistical Association, 79 (387), 516–524.

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