Package 'graphonmix'

October 9, 2025

| October 9, 2023 |
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| Type Package |
| Title Generates Mixture Graphs from Dense and Sparse Graphons |
| Version 0.0.1.0 |
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| Description Generates (U,W) mixture graphs where U is a line graph graphon and W is a dense graphon. Graphons are graph limits and graphon U can be written as sequence of positive numbers adding to 1. Graphs are sampled from U and W and joined randomly to obtain the mixture graph. Given a mixture graph, U can be inferred. Kandanaarachchi and Ong (2025) <doi:10.48550 arxiv.2505.13864="">.</doi:10.48550> |
| License GPL (>= 3) |
| Encoding UTF-8 |
| RoxygenNote 7.3.2 |
| Imports ggplot2, igraph, imager, stats |
| Suggests gridExtra, knitr, rmarkdown |
| VignetteBuilder knitr |
| <pre>URL https://sevvandi.github.io/graphonmix/</pre> |
| NeedsCompilation no |
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| Repository CRAN |
| Date/Publication 2025-10-09 07:40:02 UTC |
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```
autoplot.extract_sparse
```

Plots the output of extract_sparse function.

Description

Plots the two lines fitted to the unique, sorted log degrees of the graph.

Usage

```
## S3 method for class 'extract_sparse'
autoplot(object, ...)
```

Arguments

object The output of the function 'extract_sparse'
... Other arguments currently ignored

Value

A ggplot object.

```
library(igraph)
gr <- sample_pa(10000, power = 1.2, directed = FALSE)
sparse <- extract_sparse(gr)
autoplot(sparse)</pre>
```

create_exp_matrix 3

create_exp_matrix

Creates an nxn exponential matrix

Description

Creates an nxn matrix where the (i,j)th entry is exp(-(i+j)/scalar)

Usage

```
create_exp_matrix(nrow, scalar)
```

Arguments

nrow The dimension of the matrix scalar The scalar in exp(-(i+j)/scalar)

Value

An nxn matrix

Examples

```
W <- create_exp_matrix(100, 100)</pre>
```

empirical_graphon

Computes empirical graphon from graph

Description

Computes empirical graphon given a graph

Usage

```
empirical_graphon(gr, n = NULL)
```

Arguments

gr A graph

n Dimension of the graphon matrix

Value

The empirical graphon

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Examples

```
library(igraph)
gr <- sample_gnp(1000, p=0.2)
emp <- empirical_graphon(gr, n = 100)</pre>
```

extract_sparse

Extracts the sparse part from a (U,W) graphon mixture

Description

This function extracts the sparse component from a (U,W) mixture graph by fitting two lines to the unique sorted log degree values. The first line gives the number of hubs in the sparse part and the remaining line fits the degrees of the dense part.

Usage

```
extract_sparse(gr)
```

Arguments

gr

The input graph

Value

a list with the following components:

num_hubs The number of hubs in the sparse component.

phat The probability vector of the sparse component. This is also known as the mass

partition.

segment_sizes The sizes of the two line segments.

line_equations The two equations of the lines.

cutoff The best cut off for the two lines.

models The models of the fitted lines.

mse The mean squared error

data The degree data.

```
library(igraph)
gr <- sample_pa(10000, power = 1.2, directed = FALSE)
sparse <- extract_sparse(gr)
sparse$phat</pre>
```

generate_star_union 5

generate_star_union

Generates a sparse graph of star graphs

Description

Generates a union of star graphs given the weights

Usage

```
generate_star_union(wts, n)
```

Arguments

wts The proportion of the hub degrees

n The number of nodes in the new graph

Value

A disjoint union of star graphs

Examples

```
library(igraph)
wts <- c(0.5, 0.3, 0.2)
gr <- generate_star_union(wts, n = 100)
gr</pre>
```

graph_join

Joins two graphs

Description

Joins two graphs randomly connecting vertices

Usage

```
graph_join(gr1, gr2, p = 0.5, option = 2)
```

Arguments

| gr1 | The first graph to join |
|--------|--|
| gr2 | The second graph to join |
| р | The proportion of edges in gr1 to be added as part of the joining |
| option | Two options. 1 does the disjoint union, 2 does the random edges union. |

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Value

The joined graph

Examples

```
W <- create_exp_matrix(100, 100)
# create the sparse part - a disjoint set of stars
wts <- c(0.5, 0.3, 0.2)
grdense <- sample_graphon(W, 100)
grsparse <- generate_star_union(wts, 200)
gr <- graph_join(grdense, grsparse, opt = 2)</pre>
```

line_graphon

Creates a line graphon from a sequence of probabilities

Description

Creates a line graphon, which is a disjoint clique graphon from a sequence of probability values

Usage

```
line_graphon(probs)
```

Arguments

probs

The list of probabilities starting from the largest.

Value

The line graphon

```
library(ggplot2)
wts <- c(0.5, 0.3, 0.2)
U <- line_graphon(wts)
plot_graphon(U)</pre>
```

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plot_graphon

Plots graphon

Description

Plots graphon

Usage

```
plot_graphon(W, cols = c("white", "black"))
```

Arguments

W A graphon given by an nxn matrix cols Colors, by default white and black

Value

A ggplot object.

Examples

```
W <- create_exp_matrix(100, 100)
plot_graphon(W)</pre>
```

predict_hubs

Predicts the degree of hubs of an new graph

Description

Predicts the degree of hubs of an unseen graph given a graph generated from the same process.

Usage

```
predict_hubs(gr, n, k = NULL)
```

Arguments

gr The input graph

n The number of nodes in the new graphk The number of hubs. Default is NULL

Value

A vector of hub degrees

Examples

```
library(igraph)
gr <- sample_pa(10000, power = 1.2, directed = FALSE)
predict_hubs(gr, n = 11000)</pre>
```

sample_graphon

Generates a graph given a graphon

Description

Generates a graph given a dense graphon W.

Usage

```
sample_graphon(W, n)
```

Arguments

W A graphon given by a matrix

n The number of nodes of the sampled graph

Value

A graph sampled from the graphon W with n nodes

Examples

```
library(igraph)
W <- matrix(0.2, nrow = 100, ncol = 100)
gr <- sample_graphon(W, n= 100)</pre>
```

sample_mixed_graph

Generate a (U,W) mixture graph

Description

Generate a (U,W) mixture graph from a dense graphon W and a mass partition corresponding to a line graph graphon U.

Usage

```
sample_mixed_graph(W, wts, nd, ns, p = 0.5, option = 2)
```

scale_graphon 9

Arguments

| W | The dense graphon. This is a symmetric matrix with values in [0,1] |
|--------|---|
| wts | The degree proportions of the hub degrees. Need to add up to 1. This is the mass partition corresponding to the line graph graphon U. |
| nd | The number of nodes in the dense part of the graph |
| ns | The number of nodes in the sparse part of the graph |
| p | The nodes to be added as a proportion of the edges in the dense part |
| option | Graph joining option. If option == 1 then a disjoit union is considered. If option == 2 the two graphs are joined randomly with the number of edges specified by p. |

Value

A graph sampled from the (U,W) mixture.

Examples

```
library(igraph)
W <- matrix(0.1, nrow = 100, ncol = 100)
wts <- c(0.5, 0.3, 0.2)
ns <- 200
nd <- 100
p <- 0.5
gr <- sample_mixed_graph(W, wts, nd, ns, p, option = 2)
gr</pre>
```

scale_graphon

Scales a graphon to an nxn matrix

Description

Scales a graphon to an nxn matrix suitable for large adjacency matrices

Usage

```
scale_graphon(W, n)
```

Arguments

W A graphon given as a symmetric square matrixn The dimension of the output matrix

Value

Scaled nxn graphon

scale_graphon

```
library(igraph)
gr <- sample_gnp(1000, p=0.2)
adj <- as_adjacency_matrix(gr)
W <- scale_graphon(adj, 100)</pre>
```

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